

# Private and Stable Test-Time Adaptation with Differential Privacy

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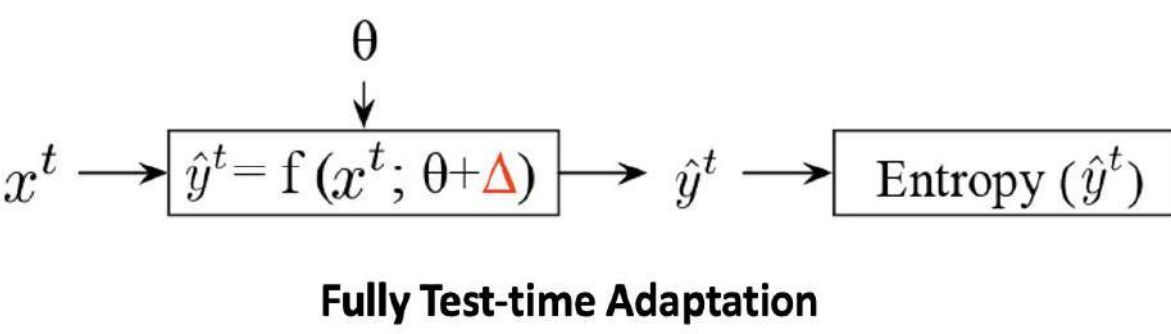
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**We make test-time adaptation private with differential privacy, and show that per-sample clipping improves both privacy and stability.**

## 1 MOTIVATION

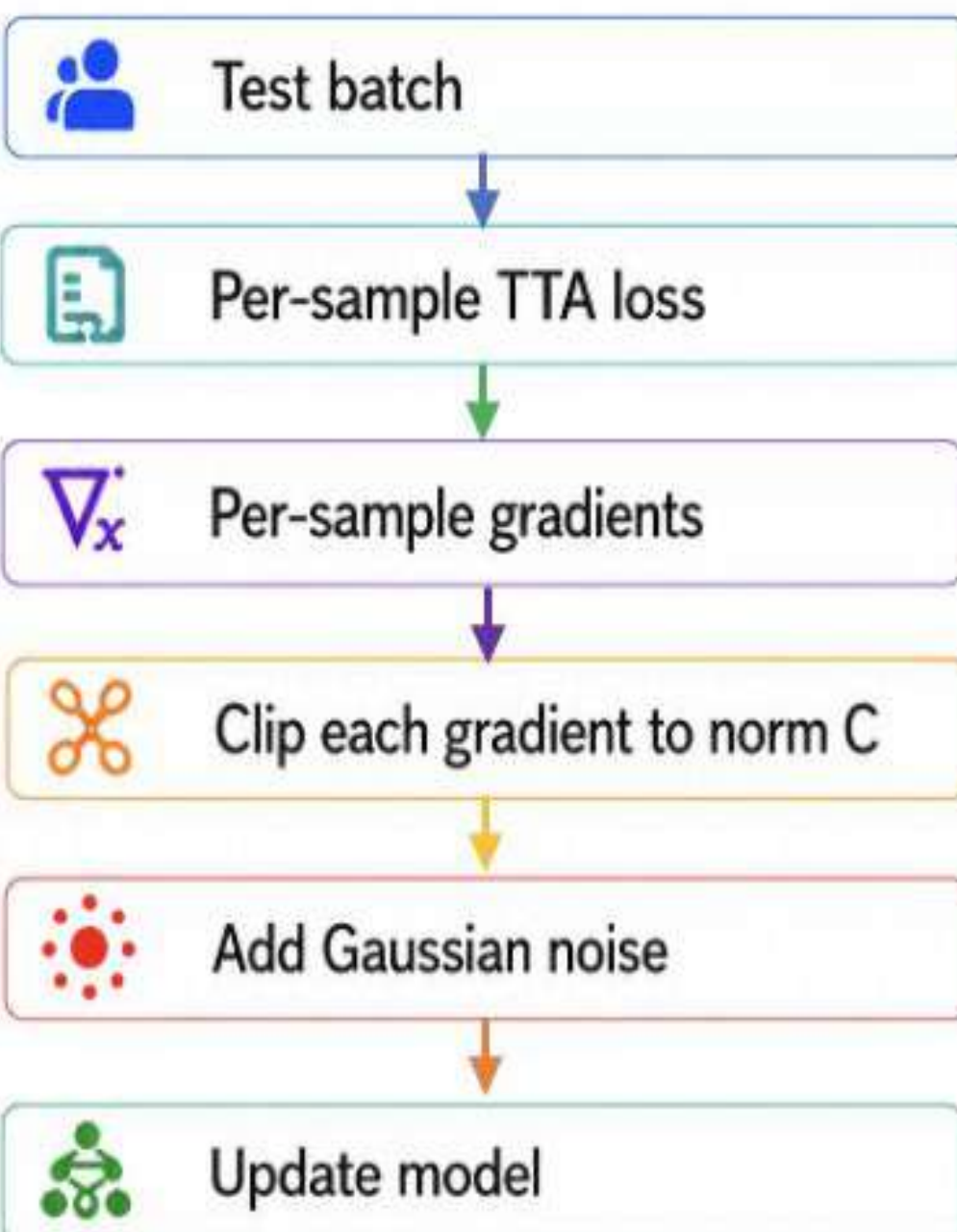
- Test-time adaptation (TTA) updates a model on unlabeled test data to recover accuracy under distribution shift.
- These updates can leak information about past test samples because model parameters depend on the test data.
- Goal: enable private, stable TTA with minimal loss in adaptation accuracy.



## 2 MAIN CONTRIBUTIONS

- Develop DP versions of Tent, EATA, SAR, DeYO, and COME.
- Show that per-sample gradient clipping is a general mechanism that improves TTA performance even without DP noise.
- Measure the privacy/accuracy trade-off for test-time adaptation in episodic and continual settings.

## 3 DP-TTA FRAMEWORK



### DP-TTA Update (per batch $B_t$ )

$$g_i(x_i) = \nabla_{\theta} \ell_{\text{TTA}}(x_i; \theta_t)$$

$$\tilde{g}_i(x_i) = \frac{g_i(x_i)}{\max(1, \|g_i(x_i)\|_2 / C)}$$

$$\Delta_t^{PP} = \frac{1}{|B_t|} \left[ \sum_i \tilde{g}_i(x_i) + \mathcal{N}(0, \sigma^2 C^2 I) \right]$$

$$\theta_{t+1} = \theta_t - \eta \Delta_t^{PP}$$

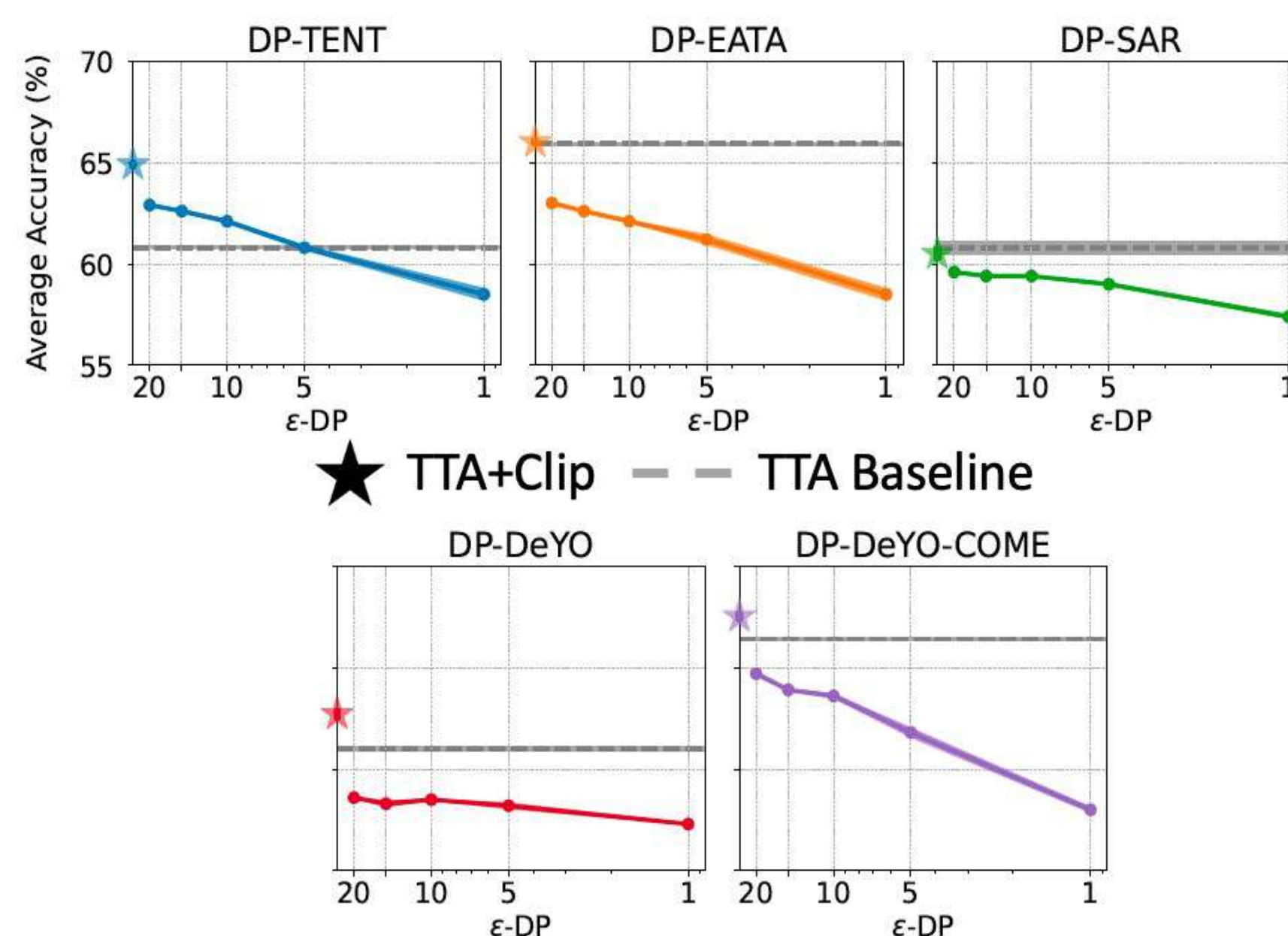
## 4 EXPERIMENTAL SETUP

- Model:** ViT-Base/16
- Data:** ImageNet-C (severity 5) + clean ImageNet-1k validation
- Settings:** episodic and continual adaptation
- Privacy budgets:**  $\epsilon \in \{1, 5, 10, 15, 20\}$ ,  $\delta = 10^{-6}$
- Batch size:** 64; per-sample clipping implemented with Opacus

## 5 PRIVACY-ACCURACY TRADE-OFF

### Average top-1 accuracy (%) on ImageNet-C (severity 5)

under different privacy budgets ( $\delta = 10^{-6}$ )



## Key Findings

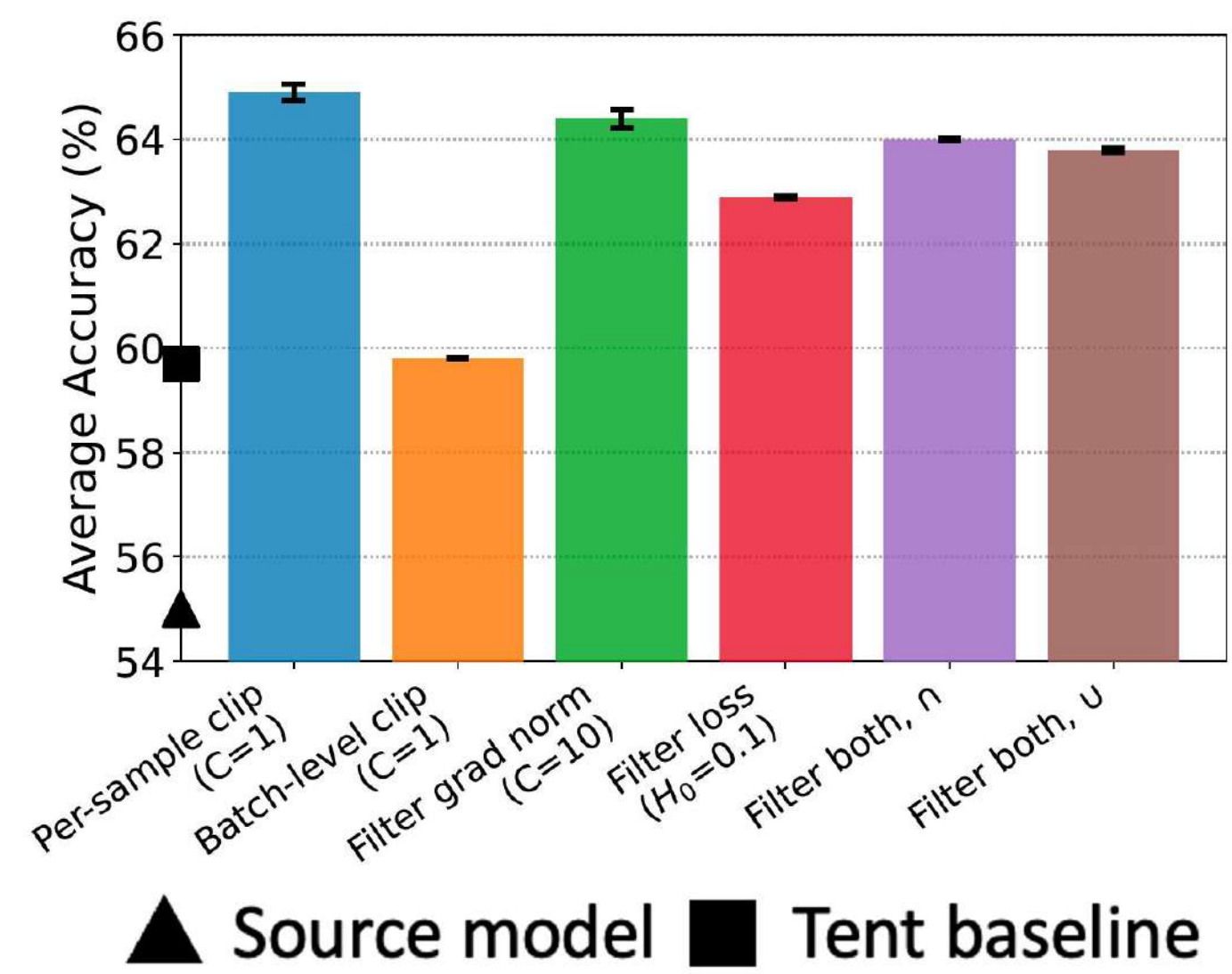
- Moderate privacy can still preserve strong adaptation performance, and some DP-TTA methods remain competitive with their non-private counterparts.
- DP-Tent is the clearest example: it achieves 62.9%, 62.6%, and 62.2% at  $\epsilon = 20, 15,$  and  $10$ , outperforming the non-private baseline of 60.8%.
- For other methods, the non-private versions remain stronger at  $\epsilon = 20$ , but the gaps are modest: 2.9 points for EATA, 1.2 for SAR, 2.4 for DeYO, and 1.7 for DeYO-COME.
- Per-sample clipping consistently improves TTA, enhancing robustness and stability, and can even yield state-of-the-art continual accuracy.

## ★ Selected quantitative results

- Per-sample gradient clipping improves adaptation across most corruption types, raising the average gain across TTA methods from **0.1%** to **4.1%**.
- DeYO-COME + clipping achieves state-of-the-art continual performance, reaching **67.5%** average accuracy.
- Per-sample clipping rescales any gradient with norm larger than  $C$  to norm  $C$ , preserving its direction while reducing its magnitude.
- Batch-level clipping is much less effective: accuracy stays around **57–59%** across thresholds  $C$ , even when the fraction of clipped batches ranges from **84%** to **1.5%**.

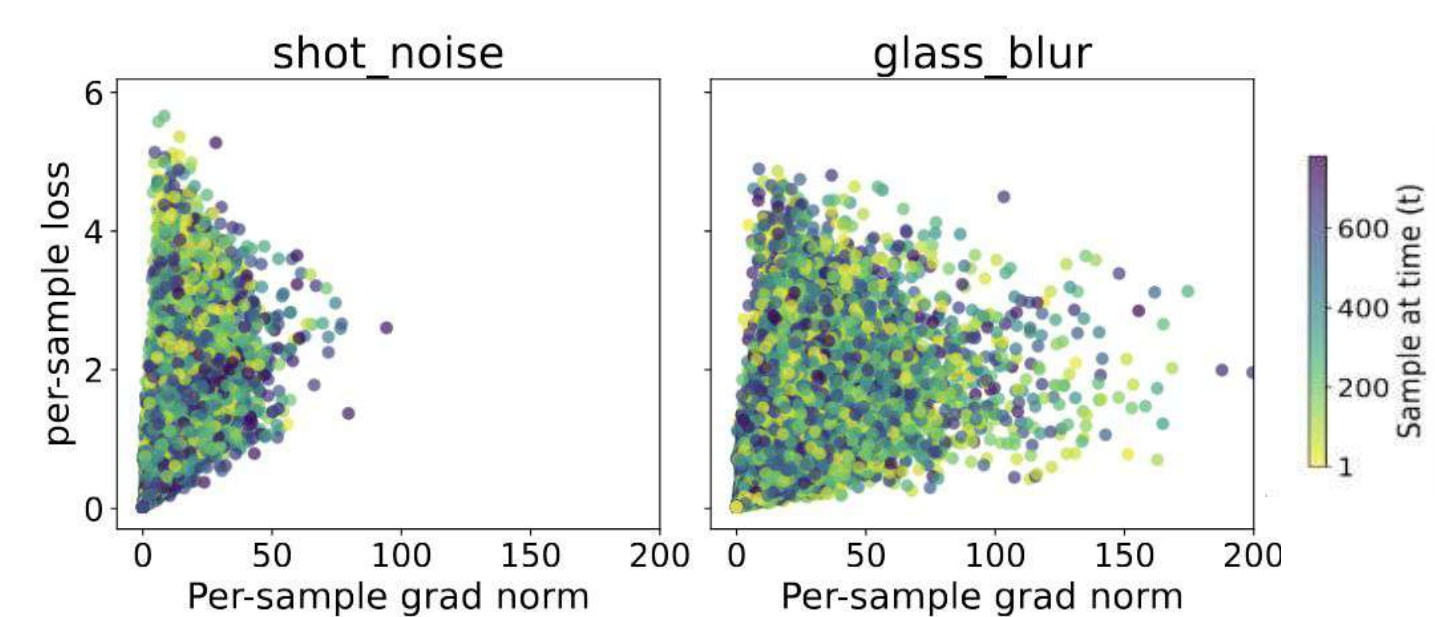
## 6 PER-SAMPLE CLIPPING IMPROVES TTA

### Per-sample Clip is better than Other Operations



- Per-sample clipping **controls per-sample influence** to model updates, batch-level clipping do not.
- Controlling per-sample influence (**clipping**) is **more efficient** than removing difficult samples (**filtering**).

### Gradient Norm and Loss Measure Different Aspect of Difficult Sample

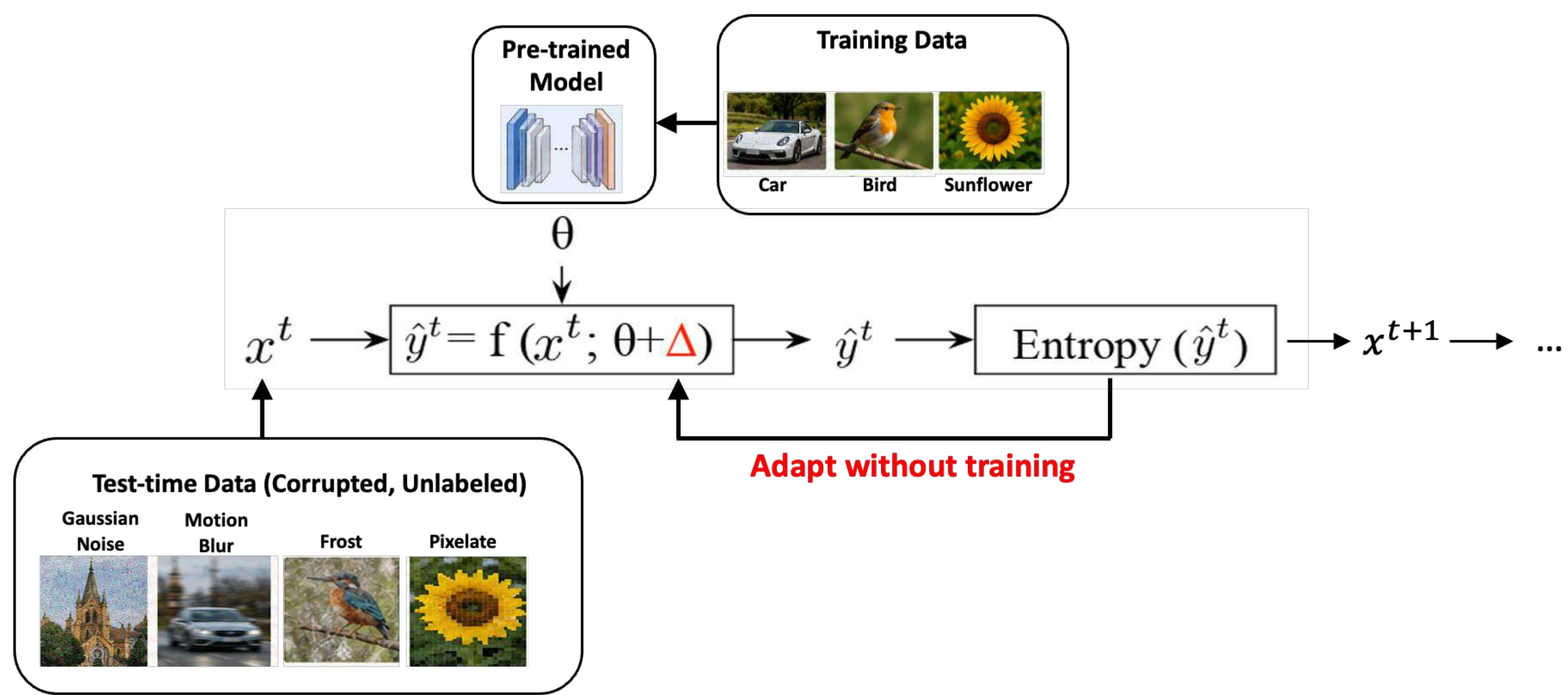


- Per-sample gradient norm and loss are **not strongly aligned**.
- They can be **complementary indicators** of difficult samples.

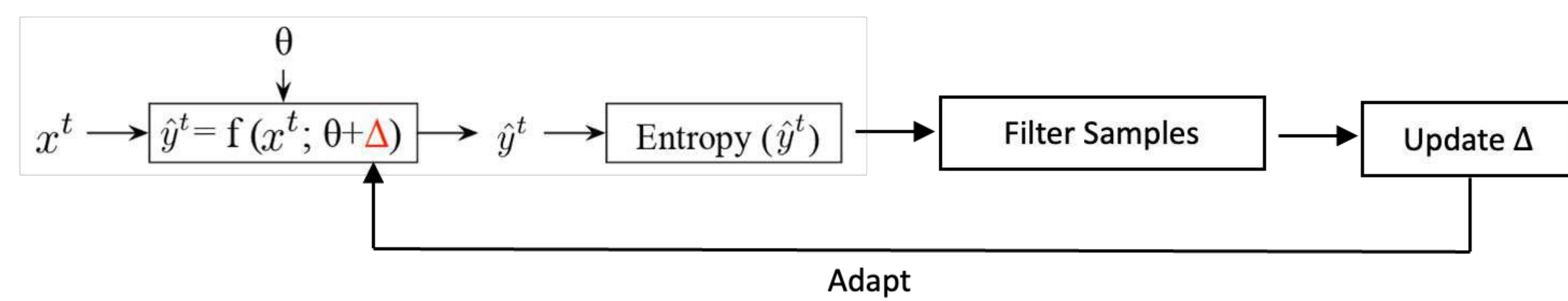
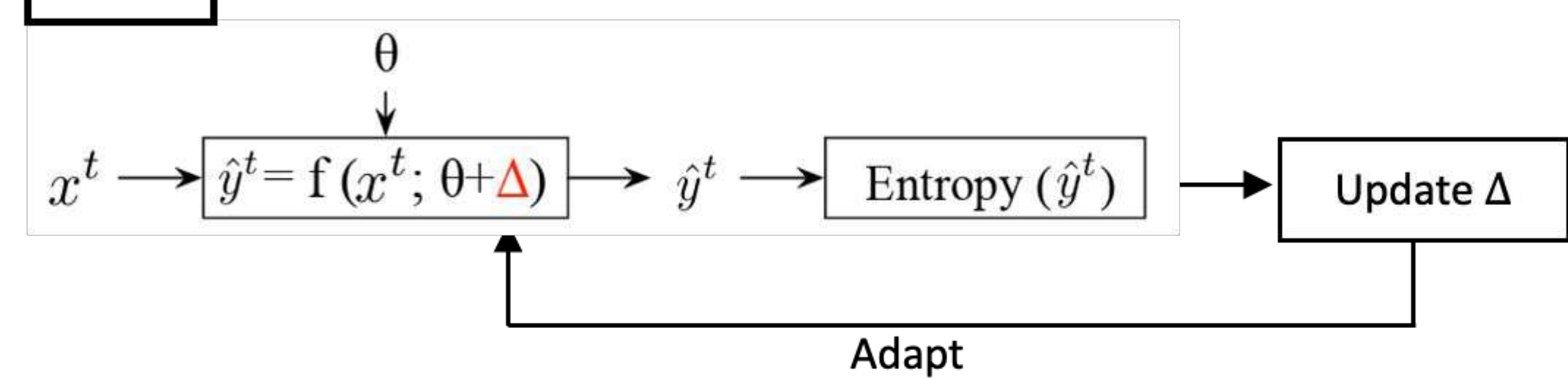
## 7 EFFICIENCY AND TAKEAWAYS

- DP adds only modest overhead: roughly 20–30 ms per batch.
- The slowest DP variant takes only 1.28x the original runtime.
- This is the first study of private test-time adaptation.
- Per-sample clipping is not only a privacy tool; it is also a strong stability mechanism for TTA.
- Private test-time updates remain practical and effective.

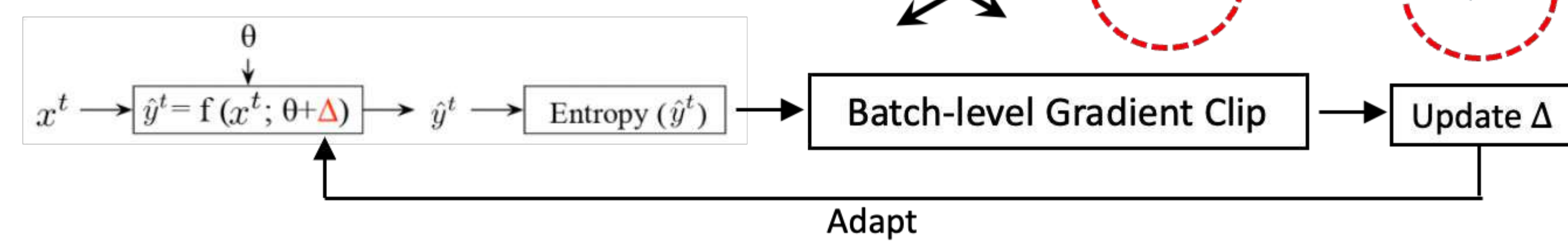
**Key message:** Private TTA is practical and effective, with modest overhead; per-sample clipping improves privacy and stability.



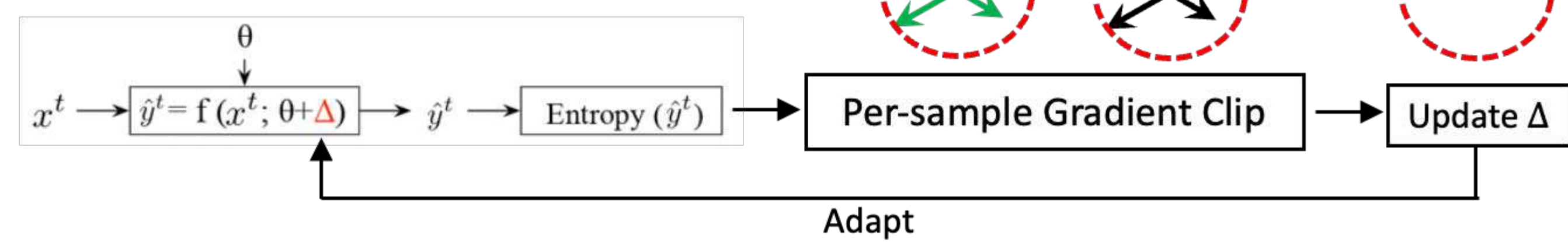
**TTA**



**TTA + Batch Clip**



**TTA + Per-sample Clip**



**DP-TTA**

